Exercise Class 2

Exercise 1

Consider a state $|\psi\rangle$. Knowing that $P_0(|\psi\rangle) = 0.933, P_1(|\psi\rangle) = 0.067, P_0(H|\psi\rangle) = 0.625$, $P_1(H|\psi\rangle) = 0.375, P_0\left(HS^\dagger|\psi\rangle\right) = 0.7165, P_1\left(HS^\dagger|\psi\rangle\right) = 0.2835$, estimate the angles θ, ϕ localizing the state on the Bloch sphere.

Exercise 2

Consider the truth table:

Input state $\|\psi_{in}\rangle$	Output state $\|\psi_{out}\rangle$
$\|0\rangle$	$\|-\rangle$
$\|1\rangle$	$\|+\rangle$

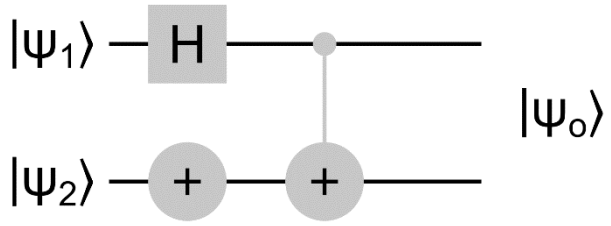
Calculate the operator $\hat{O}$ such that $|\psi_{out}\rangle = \hat{O}|\psi_{in}\rangle$.

Exercise 3

Consider a two-qubit system with state $|\psi\rangle = \frac{1}{\sqrt{2}}(|01\rangle - |10\rangle)$. Determine whether the state is a *product state* or *entangled state*.

Exercise 4

Consider the two-qubit circuit in Fig. 1, where input qubits $|\psi_1\rangle, |\psi_2\rangle$ are prepared in the $|0\rangle$ and $|1\rangle$ state respectively. Determine the output state $|\psi_o\rangle$ of the circuit.



Exercise 5

Consider the two-qubit circuit in Fig. 1. Determine the truth table and the corresponding equivalent operator $\hat{O}$.